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The product of shape fibrations

The notion of shape fibration for maps between metric compacta was introduced by S. Mardešić and T. B. Rushing in [4] and [5]. In [3] S. Mardešić has extended this notion to maps of arbitrary topological spaces. The author has established some further properties of shape fibrations in the noncompact case (see e.g. [1], [2]).

The main result of this paper is the following theorem: *If $p : E \rightarrow B$, $p' : E' \rightarrow B'$ are maps of arbitrary topological spaces E, E' to compact Hausdorff spaces B, B' , then $p \times p' : E \times E' \rightarrow B \times B'$ is a shape fibration if and only if p and p' are shape fibrations.* T. Watanabe in [6] has proved that the product of maps between compact Hausdorff spaces is a shape fibration if and only if each of these maps is a shape fibration. Thus, our result can be considered as a generalization of the above mentioned Watanabe's result.

In order to obtain our main result, we have also shown the following result about resolutions of product spaces: *Let $\mathbf{q} = (q_\lambda) : E \rightarrow \mathbf{E} = (E_\lambda, q_{\lambda\lambda'}, \Lambda)$ be a morphism of **pro-Top** and $\mathbf{r} = (r_\mu) : B \rightarrow \mathbf{B} = (B_\mu, r_{\mu\mu'}, M)$ a morphism of **pro-Cpt** such that \mathbf{E} is an ANR-system and \mathbf{B} a compact ANR-system. Then $\mathbf{q} \times \mathbf{r} = (q_\lambda \times r_\mu) : E \times B \rightarrow \mathbf{E} \times \mathbf{B} = (E_\lambda \times B_\mu, q_{\lambda\lambda'} \times r_{\mu\mu'}, \Lambda \times M)$ is a resolution of $E \times B$ if and only if \mathbf{q} and \mathbf{r} are resolutions of E and B respectively.*

References

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